

Does Inter-Market Competition Lead to Less Regulation?¹

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Abstract

This paper presents a model to analyze the consequences of competition in order-flow between a profit maximizing stock exchange and an alternative trading platform on the decisions concerning trading fees and listing requirements. Listing requirements, set by the exchange, provide public information on listed firms and contribute to a better liquidity on all trading venues. It is sometimes asserted that competition induces the exchange to lower its level of listing standards compared to a situation in which it is a monopolist, because the trading platform can free-ride on this regulatory activity and compete more aggressively on trading fees. The present analysis shows that this is not always true and depends on the existence and size of gains related to multi market trading. These gains relax competition on trading fees. The higher these gains are, the more the exchange can increase its revenue from listing and trading when it raises its listing standards. For large enough gains from multi-market trading, the exchange is not induced to lower the level of listing standards when a competing trading platform appears. As a second result, this analysis also reveals a cross - subsidization effect between the listing and the trading activity when listing is not competitive. This model yields implications about the fee structures on stock markets, the regulation of listings and the social optimality of competition for volume.

Keywords: competition in order flow, fragmentation, listing requirements, stock exchanges

JEL classification: G10, G18, G12

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1. Introduction

This paper explores how multi-market trading affects the optimal decisions of profit maximizing exchanges on listing requirements in connection with trading fees and listing fees. Over the last two decades exchanges have increasingly been transformed into demutualised and listed firms the decisions of which are based on the principle of profit maximization. Many of them have retained or acquired discretion on listing standards. Furthermore, alternative trading systems have emerged since the 70's in the US but very recently in Europe, and compete for volume with "traditional" stock markets without listing firms themselves.³ In this paper, a model is established to analyze whether competition for order flow between a "traditional" exchange and a trading platform leads to a lower level of listing requirements.

If an exchange regulates listings, competing trading platforms can free ride on this regulatory activity while offering more advantageous trading conditions. The exchange, which does not internalize the profit of trading platforms and faces competition on trading fees, might be induced to reduce the level of listing requirements. The results of the present analysis show that competition in volume does not necessarily reduce the level of listing standards set by an exchange as compared to the case in which the latter is a monopoly. If different trading venues compete for order-flow, investors incur smaller trading costs due to lower trading fees and because investors benefit from a smaller price impact when they can trade on several trading venues. This, in turn, leads to a larger share issue on the exchange. Not only does competition alter the distribution of volume, it also increases the total volume and contributes to raising the listing fee the exchange can charge. These effects might increase the marginal gain the exchange obtains from raising listing standards and might lead to a higher level of listing requirements than the one that obtains in a monopoly situation. This finding is in contrast to what the free-rider logic suggests.

The model developed in this paper is based on the following assumptions: The owner of a firm with a value unknown to market participants lists the firm on a stock exchange to sell a fraction of his shares to two outside investors. At a later period, these investors might trade. The investors can trade on a stock exchange or on an alternative trading platform. On both venues, they trade with a risk averse market maker, which creates a price impact corresponding to the risk premium of the market makers. At the IPO stage the investors discount the IPO price they are willing to pay by an amount corresponding to the expected

³ These alternative trading systems are for instance electronic order books such as Chi-X or Island which offer to organise trading in the shares of large firms listed on stock exchanges.

price impact. The listed firm must commit to listing requirements that oblige the firm to disclose noisy information about its productivity after it undertook the IPO, and to thereby reduce information asymmetry. The firm bears also compliance costs that increase with the level of listing requirements. Both trading venues charge a fee per traded share and determine this fee to maximize their respective profits. In addition, the exchange charges a listing fee which is proportional to the surplus net of costs that the owner of the firm earns by undertaking the listing. The exchange determines the level of listing requirements to maximize its profit.

Consider first an exchange which is a monopoly, both in listing and in trading. Higher listing requirements reduce the trading costs that investors expect to incur. This translates into a higher IPO price inducing the owner of the firm to sell more shares, to the extent that the gain from smaller trading costs is not offset by the additional compliance costs. In this case, his surplus also increases. As a consequence, the exchange benefits from a higher level of listing requirements both through a larger income from trading and through a larger income from listing. The optimal level of listing requirements is reached when the marginal increase in compliance costs offsets these marginal gains.

In the case in which a trading platform competes for volume with the exchange, both the pressure this competition induces on the trading fees, and the smaller price impact investors can obtain due to multi-market trading, increase the IPO price. This leads to a higher number of issued shares and thus a higher volume on the secondary market as well as a higher surplus for the initial owner of the firm. In this situation, an increase in the level of listing requirements has two effects: it reduces the size of the price impact faced by investors on both trading venues intensifying thereby competition on trading fees, and it reduces overall trading costs leading to a higher number of issued shares and thus to an increase in the revenue from trading and from listing. When the competition effect on trading fees dominates, the exchange cannot benefit from these welfare effects. Its marginal gain from increasing listing standards is smaller than in the monopoly case and it sets a smaller level of listing requirements in equilibrium. If, in contrast, the competition on trading fees is weak, the marginal revenue that the exchange obtains from raising the listing standards is larger than in the monopoly situation even though the exchange loses a fraction of the volume. This is due to the possibility to set a higher trading fee and occurs when the price impact faced by investors is large (i.e. when the incentive to trade on both venues is strong). As a consequence the exchange is induced to increase the level of listing requirements compared to the monopoly situation.

The main contribution of this paper is to show that the effect of competition for trading volume on the regulatory activity of a self-regulating exchange regarding listings depends on whether competition is mainly driven by trading fees or by gains related to the fragmentation of order-flow. In the academic literature there is a controversial debate about the reasons for order-flow fragmentation and its consequences on market quality.⁴ The present analysis shows that uncovering the reasons for fragmentation of order flow is essential for the assessment of the consequence of competition in volume on the regulatory activity of a “traditional” stock exchange. The existing literature also mainly focuses on the consequences of multi-market trading on the behavior of traders and considers stock exchanges as given institutions. The present paper pushes the analysis further by considering the impact of multi-market trading on the decisions of stock markets.

Listing requirements affect the utility of investors and the profit of additional trading venues. If they are determined by the exchange, they are sub-optimal from a social point of view since the exchange bears a part of the regulatory costs but internalizes neither the changes in the utility of investors nor the gains of the trading platform. The problem of non internalized benefits related to listing requirements can be solved partially by merging the exchange with the trading platform: While the extent to which regulation is sub-optimal becomes smaller due to the merger, the merged entity increases the trading fee due to the lack of competition. Also, the decision about the level of listing requirements depends again on the factors driving order-flow fragmentation.

As a second result, this paper reveals the existence of an interdependence between the listing fee charged only by the exchange, and the trading fees set by all trading venues, i.e. both the exchange and the competing alternative trading platform. Smaller trading fees increase the surplus of the owner of the firm and lead thereby to an increase in the listing fee. This effect leads to a lowering of the trading fee set by the exchange. In the case of competition for volume, this interdependence triggers price competition between the trading venues. Consequently, the association of listing and trading in one profit maximising entity leads to smaller average trading costs as compared to a case in which listing and trading are separated.

One way which has been proposed to mitigate the supposed problem of under-regulation related to competition in volume consists of separating listing from trading completely so that exchanges only provide liquidity but have no discretion on listings (Macey

⁴ See Pagano (1989b), Gajewski and Gresse (2007), Foucault and Menkveld (2008), O’Hara and Ye (2009), Chowdry and Nanda (1991), Madhavan (1995), Foucault and Gehrig (2008)

and O'Hara 2005). Many other reasons might also justify a separation of these functions.⁵ The economic objectives of the listing and trading functions can be achieved through different organisational settings, including settings, in which they are carried out by different independent organisations. However, the present analysis shows that bundling the listing and trading functions on one single exchange or separating them into several independent organisations has substantial impacts on the price structure of the services provided in relation to these functions.

These findings are of particular interest when considering the recent evolution in the stock market industry. The demutualisation process of stock exchanges has brought about changes in the competency of some stock exchanges with regard to listing conditions. While some exchanges have lost discretion on listings, others have kept or even acquired the right to regulate listings autonomously.⁶ The variety of existing organisational models shows that there is no consensus among policy makers regarding self regulatory competencies of exchanges. These developments have triggered a debate in the professional and the legal academic literature about whether stock exchanges should continue to regulate listings.⁷ The reasons mentioned in favor or against regulation of listings by stock exchanges are based on arguments developed in the literature on self-regulatory organizations.⁸ They are related, among other things, to the incompatibility of listing regulation with the objective of profit maximization or to the necessity to sustain the confidence of investors specifically in a competitive environment.

While the debate about regulatory competencies of stock markets is strong in the legal literature, only a small number of studies in economics and finance analyze the economic rationales behind choices of self-regulating and profit-maximizing exchanges. Chemmanur and Fulghieri (2006) analyze how profit maximizing exchanges set optimal listing requirements and suggest that exchanges are induced to set a high level of listing requirements because this allows them to build and to sustain a good reputation. In

⁵ Other reasons are related to the existence of conflicts of interests, anti-competitive behaviour, the lack of incentives to enforce listing requirements as well as the rise of other institutions which compete with exchanges in different services and might be more efficient than exchanges. See Fleckner (2006), Lee (2002), Macey and O'Hara (2002, 2005), Macey et al. (2005).

⁶ Firms wishing to trade on the London Stock Exchange and the Hong Kong Stock Exchange need first to be listed by the respective independent authority, the Financial Services Authority and the Securities and Futures Commission. Euronext has remained self-regulating while Deutsche Börse has acquired the right to determine listing rules in 2002. The NYSE has separated the entire regulatory activity from other operations. This activity is now carried out by a separate entity.

⁷ Fleckner (2006), Macey and O'Hara (2005), Macey and O'Hara (2002), Lee (2002), Steil (2002), Centre for financial market integrity (2007), OICV – IOSCO Consultation Report (2006)

⁸ See for instance DeMarzo et al. (2005)

Chemmanur and Fulghieri's model listing requirements refer to the efficiency with which the exchange selects the firms it lists. In the present paper, in contrast, listing requirements constitute a commitment of the firm to reveal information. Also, the authors only consider competition in listings and trading does not occur, while the present study analyses both listing and trading.

Competition in trading in relation with disclosure requirements is addressed in Huddart et al. (1999). In their model, managers who list their firms also possess private information which they want to exploit by trading their shares. Liquidity concentrates on the exchange with the highest disclosure standards due to smaller adverse selection costs. Managers prefer to list their firms on this exchange although they cannot exploit their private information. This induces exchanges competing for listings and for trading volume to set high levels of listing requirements and to "race to the top". The present paper displays major differences compared to Huddart et al. (1999). While in Huddart et al. liquidity concentrates on one exchange, the present paper allows for endogenous fragmentation of volume. Also, exchanges in Huddart et al. maximize only volume. In the present paper, the exchange obtains revenue from both, listing and trading, and the alternative trading platform has revenue only from trading. Therefore, the model presented in this paper is more realistic in that it considers the decisions of trading venues also on listing and trading fees and not only on volume.

This paper also relates to literature dealing with the price structure on stock markets. The linkage between listing and trading fees is studied in Foucault and Parlour (2004). The authors show that where firms differ in productivity, highly productive firms prefer to list on an exchange with a high listing fee and a small trading fee while firms with a low productivity have the reverse preference. This is because highly productive firms issue a higher number of shares. They need to attract investors with a shorter expected horizon, and are therefore more sensitive to the level of trading costs. In Foucault and Parlour (2004), two competing exchanges differentiate in trading and in listing fees and the equilibrium structure of these fees depends on the profile of the firms which the exchanges attract as clientele: An exchange listing firms with a high productivity will set a high listing fee and a small trading fee in equilibrium. While competition for volume affects the price structure, the authors consider in particular the listing decisions of firms and assume that the shares are traded on the exchange on which the firms are listed. In addition, the authors do not analyze listing requirements.

The article proceeds as follows. Section 2 sets out the model. Section 3 analyses the trading round and the IPO stage. Section 4 analyses of the decisions of a monopoly exchange on the trading fee and the level of listing requirements as a benchmark case. Section 5 carries

out the analysis of competition for volume. Section 6 extends the analysis by considering the social desirability of competition in volume, the social optimality of listing requirements when they are privately determined by a stock market and the influence of differently informed investor bases on the main result. Section 7 presents the implications of the analysis developed in the previous sections and formulates conclusions. Proofs are given in the appendix.

2. Model

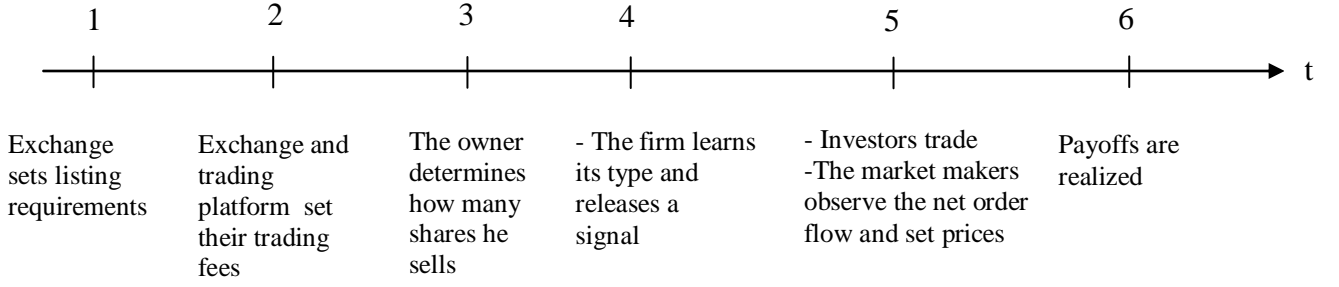
The game is organized in six stages. Time is not discounted. There is a firm initially entirely owned by a private financier (a venture capitalist for example) who is called “the owner” in what follows. The owner sells a fraction of his shares to two large outside investors by listing the firm on a stock exchange. At a later period, these investors can be hit by a liquidity shock or observe private information about the firm. They can trade their shares on the stock exchange or on an alternative trading platform. Trading is intermediated by competitive market makers. All agents are risk neutral except the owner and the market makers who are risk averse.

The timing of the model is illustrated in figure 1. In the two first stages, the exchange determines its listing and trading conditions. First, it sets a level of listing requirements. This decision is considered as a long term decision since it implies the setting up of particular listing procedures as well as of specialized departments to enforce these requirements.⁹ Second, the exchange sets the trading fee. This decision is considered as short term decisions since fees can be changed quickly.¹⁰ At the third stage, the owner of the firm determines how many shares to sell to the outside investors. At this stage, the future cash flows of the firm are unknown to all agents. At the fourth stage, the firm learns the value of future cash flows. To comply with listing requirements the firm releases a noisy signal about its value. At the fifth date, one of both investors might be hit by a liquidity shock and might sell his entire holding. The other investor might observe perfectly the value of the future cash flows of the firm and might trade to exploit this information. Finally payoffs are realized. The equilibrium concept is sub-game perfection. The model is solved by backward induction.

⁹ Listing requirements can also contribute to the reputation of the exchange (Chemmanur and Fulghieri (2006)) and are therefore taken in a long term perspective.

¹⁰ Foucault and Parlour (2004) analyze the decisions of exchanges on listing fees and trading technologies sequentially. Competition in listing fees represents short run competition and occurs in the second stage of their model while competition in trading technologies represents long run competition and occurs at the first stage.

Figure 1: extensive form of the game



2.1. The firm

We consider a firm with assets in place. Initially, the firm is completely owned by a private financier or an entrepreneur who has invested an amount K in the firm at an earlier stage not analyzed explicitly in this model. We assume that the owner holds K shares which he has bought for 1 monetary unit each.¹¹ The firm realizes a project which yields a payoff of $V = 1 + x$ per monetary unit invested by the owner, and thus per share, where x is a random variable taking two equally likely values: x_h and x_l with $x_h > x_l > 0$. Shares are divisible so that fractions of a share can be traded.

The owner of the firm is characterized by a mean variance utility, U . At $t = 3$ he lists the firm on the exchange and sells a fraction, $\alpha \in (0,1)$, of his shares to outside investors at the share price, P_{IPO} . He determines the fraction of shares to be sold to maximize his utility:

$$\text{Max}_{\alpha} \alpha K P_{IPO} + (1 - \alpha) K E[V] - \frac{\rho}{2} (1 - \alpha)^2 K^2 \sigma_V^2, \quad (1)$$

where ρ measures his risk aversion, $E[V] = 0.5(x_h + x_l)$ is the expected value per share and $\sigma_V^2 = 0.25(x_h - x_l)^2$ is the variance of the value. The utility of the owner if he does not sell shares is:

$$\bar{U} = K E[V] - \frac{\rho}{2} K^2 \sigma_V^2 \quad (2)$$

The surplus he obtains when he lists the firm and sells a fraction α of his shares, is:

$$\Delta U(\alpha) = U(\alpha) - \bar{U} \quad (3)$$

¹¹ A similar normalization is used in Foucault and Parlour (2004), where investors can buy shares for 1 monetary unit.

At the time of listing, x is unknown to all agents. Therefore, the listing decision alone does not convey information about the quality of the firm to the market.¹² The firm learns the value of the project after the shares are floated but before trading takes place. However, it cannot credibly convey this information to market participants. It remains its private information. This hypothesis is necessary, because the model relies on the existence of information asymmetry.

2.2. The stock market industry

We assume that there is a stock market listing the firm and organizing trading in the shares. It is a monopolist in listing. There is also a trading platform which does not operate listings but offers only to trade the shares of the firm listed on the exchange. In what follows, the stock market operating listings is called “the exchange” whereas the market operating only trading in the listed shares is called “the trading platform”. All variables related to the exchange have a subscript e , and those related to the trading platform have a subscript pl .

The exchange sets listing requirements, which are a set of rules to which the listed firm must adhere. These rules contain accounting and reporting standards but also corporate governance mechanisms which, if in place, reveal information about the value of the firm. Listing requirements lead to a noisy public signal, s , about the value of the firm, which is observed by all market participants. The observed signal corresponds to the true value with probability $\theta \in (0.5, 1)$; it corresponds to the wrong value otherwise. The precision of the signal, θ , represents the strictness of listing requirements: the more stringent they are, the higher is the probability to observe the true value of the firm. The signal is expected to take either value, x_h or x_l , with a probability of $1/2$. The listed firm bears compliance costs when it releases the required information: $C(\theta)$ with $C' > 0$ and $C'' > 0$.

Both trading venues charge a trading fee per share traded on the secondary market, f_e and f_{pl} .¹³ The exchange also charges a listing fee, F , paid by the owner of the firm when he

¹² In a different set up in which the firm knows its type before it takes the decision to list, Stoughton et al. (2001) show the existence of separating equilibria in which only good firms list and reveal perfectly their type. The results in this paper rely on the existence of information asymmetry and would also hold if listing were informative as long as the type of the firm is not revealed perfectly. Similarly, a noisy signal at the IPO about the type of the firm would not change the results.

¹³ The structure of trading fees differs among stock exchanges. Many charge fees that are proportional to the value traded. However, some also charge fees per order or per share. The assumption made here, that trading fees are proportional to the number of traded shares and not to the transaction value keeps the analysis tractable.

lists the firm. We assume that the listing fee is the outcome of some exogenous bargaining between the owner of the firm and the exchange. It is a fraction, $\nu \in (0,1)$, of the owner's surplus net of compliance costs.¹⁴ Since the owner holds $(1-\alpha)$ of the shares, he anticipates that his final total payoff is reduced by the same fraction of compliance costs. The listing fee is:

$$F = \nu(\Delta U(\alpha) - (1-\alpha)C(\theta)) \quad (4)$$

This assumption is important for what follows, it is hinged upon the assumption that listing is not competitive. Some observations might justify this. First, competition for listings on an international level seems to be limited to a small number of firms. Also, these firms prefer to cross-list rather than to do an IPO directly on a foreign exchange.¹⁵ Second, on a regional or national level, exchanges competing for listings are rare when we look outside the US.¹⁶ From a practical point of view, some exchanges discriminate through prices with a listing fee schedule depending for instance on the market value or on the number of shares of firms. Other exchanges impose fixed listing fees, independent of the size of firms.¹⁷ The results of this model hold with different fee structures, as long as the revenue that the exchange obtains from listing depends on the listing or share issue decisions of the firm.

The level of listing requirements, θ , and the trading fees are determined by the exchange and by the trading platform to maximize their respective expected profit. As stock markets are increasingly transformed into demutualised and listed entities, the objective of profit maximization seems relevant.

2.3. Investors

Two large investors participate in the IPO of the firm. Each of them buys half of the offered shares. At $t=5$, one of both investors suffers a liquidity shock (henceforth the "liquidity trader"). With probability $\frac{1}{2}$ this investor must sell his entire holding at this stage.

¹⁴ If the firm had no bargaining power, the exchange would charge the entire surplus of the owner.

¹⁵ Some Israeli high-tech firms listed directly in the US instead of on their home market (Blass & Yafeh (2001)). This however, constitutes an exception. See Karolyi (2006) for an overview of the literature on cross-listings.

¹⁶ As an example, there are only two German firms cross-listed on the European regulated markets operated by the group NYSE Euronext and two French firms cross-listed on the regulated market of Deutsche Börse.

¹⁷ The NYSE, for instance, charges a listing fee which is proportional to the number of issued shares (see the Listed Company Manual, www.nyse.com). Deutsche Börse imposes a fixed annual fee which is independent of the size of listed firms or of the number of shares issued (see <http://deutsche-boerse.com>).

Otherwise he does not trade.¹⁸ At the same time, the other investor observes the true value of the firm with probability 1 and trades to exploit this information (henceforth the “informed trader”). At the IPO (in $t = 3$), the investors do not know their type. They expect to become a liquidity trader with probability γ .

Both investors can trade on the exchange and on the trading platform. On both trading venues, they trade with a competitive market maker characterized by a mean-variance utility. Market makers do not pay trading fees. This assumption is consistent with the current policy of many trading venues to impose reduced trading fees, or not to impose trading fees on liquidity suppliers.¹⁹ The market makers determine the bid price they are willing to pay for a given number of shares according to the public signal and to the total order-flow they observe. They equalize the transaction price to the utility they obtain from trading in the shares of the firm. The bid price for a total order-flow Q , $P_B(Q)$, and given signal, s , is determined as follows:

$$P_B(Q) = E[V|s, Q] - \frac{\lambda}{2} Q \text{Var}[V|s, Q], \quad (5)$$

where λ measures the risk aversion of the market maker, $E[V|s, Q]$ and $\text{Var}[V|s, Q]$ are the expected value of a share and the variance of the value respectively, both conditional on the public signal and on the observed total order-flow. If the market makers buy shares, the bid price at which investors can sell these shares decreases with the number of traded shares, unless the market makers can infer the true value of the firm from the order-flow or the signal.

This possible price impact might induce investors to split their orders across the two trading venues. Investors execute a fraction β of their order on the trading platform. They determine β to maximise the proceeds they obtain from trading. The public signal released by the firm is observed on both trading venues. As a consequence, the price obtained by investors on the trading venues differs only in the price impact if the submitted orders are of a different size. The trading venues only differ in trading fees. Orders are submitted to minimize the costs stemming from the expected price impact and from the trading fees. For a quantity Q sold by investors, the objective function is:

¹⁸ This assumption that the liquidity trader does not trade with probability $\frac{1}{2}$ is made for simplicity. The model also holds if the liquidity trader sold a different number of shares.

¹⁹ If market makers paid trading fees, they would pass it through to the transaction price and these fees would eventually be borne by investors. The results of the analysis would not change qualitatively in such a case.

$$\text{Min}_{\beta} \beta f_{pl} + (1-\beta)f_e + \phi \frac{\lambda}{2} \text{QVar}[V|s](\beta^2 + (1-\beta)^2) \quad (6)$$

where ϕ represents the probability that the market maker does not infer the true value of the firm given signal s , and $\text{Var}[V|s] = \theta(1-\theta)(x_h - x_l)^2$ is the variance of the value given the public signal.

3. Trading and IPO

Trading price. This sub-section examines how the price is set in $t = 5$. The precision of the public signal released by the firm prior to the trading round indicates not only the possible value of the asset, but also the probability with which the informed trader has the same information as the one observed by the other market participants. If the market maker has observed a good signal (x_h), he knows that the signal is correct with probability θ . Thus, with probability θ the informed trader also knows that the firm has a high value. If the market maker has observed a bad signal (x_l), he knows that it is correct with probability θ . Thus, with probability θ the informed trader also knows that the firm has a low value.

The informed trader always imitates the liquidity trader and sells his entire holding, $0.5\alpha K$, if he trades. He also splits his order across the two trading venues in the same way as the liquidity trader to remain hidden. If the informed trader submits orders of different quantities to the market makers, he is recognized and cannot benefit from his private information. The market makers on both trading venues face a signal extraction problem. Consider the market maker on the exchange (the logic is identical for the market maker on the trading platform). A total net order flow of $-(1-\beta)0.5\alpha K$ is obtained if the informed investor knows that the firm has a high value. In this case, the order-flow stems from the liquidity trader. The same net order-flow is obtained when the liquidity trader does not trade and the strategic trader knows that the firm has a low value. Since the market maker cannot infer the quality of the firm from the order flow in these situations, he bears a risk from holding the shares. He sets the price equal to the expected value per share minus his risk premium per share conditional on the public signal:

$$P_B = E(V|s) - \frac{\lambda}{2} (1-\beta)0.5\alpha^* K \text{Var}[V|s] \quad (7)$$

If the firm has a low value and the liquidity trader trades, the market maker observes a net order flow of $-(1-\beta)\alpha^*K$ and infers from this observation that the firm is bad. If the firm has a high value and the liquidity trader does not trade, there is no trading volume.

The price, at which the liquidity trader expects to sell his shares in the case of a liquidity shock, is below the expected value of the asset, since the market maker bears a risk premium when information remains asymmetric, and he takes into account the possibility of informed trading. The expectation of the bid price on the exchange over the signal and the probability of informed trading is the expected value of the shares reduced by a spread composed of an information component, S , and the risk premium of the market maker, $RP * Q_e$:

$$E[P_B] = E(V) - S - \frac{1}{2} RP * Q_e \quad (8)$$

where $S = (1-\theta)\theta(x_h - x_l)$, $RP = \frac{\lambda}{2} Var[V|s]$ and $Q_e = (1-\beta)0.5\alpha^*K$. See appendix A1 for the derivation of equation 8. The expected bid price on the trading platform is similar and differs only in the price impact related to the risk aversion of the market maker which is determined by $Q_{pl} = \beta 0.5\alpha^*K$. The expected value of the asset is discounted by the adverse selection costs, S , borne by the liquidity investor which accounts for the presence of the informed trader on the market. A more volatile asset leads to a less accurate price on average. A more precise signal reduces the information gap between the market maker and the informed trader, which reduces the adverse selection cost. The signal precision also determines the uncertainty about the value of the asset and thus the risk premium of the market maker. More precise information reduces the conditional variance of the payoff and thereby the risk premium and the price impact. It follows that a higher level of listing requirements improves the liquidity by reducing the adverse selection costs and the price impact borne by the liquidity trader.

When $\theta = 1$, uncertainty about the firm is completely removed and investors expect to sell their shares at the true value. The spread is zero. If $\theta = 0.5$, the public signal is completely uninformative. The spread is at its highest value.

Fragmentation. When $\lambda > 0$ and $\theta < 1$, investors expect to bear a price impact due to the limited absorption capacity of the trading venues. This might induce them to split their orders across the two trading venues. If the order-flow is fragmented, each market maker buys a smaller amount of shares and the total price impact faced by investors is smaller compared to the situation in which the entire flow is directed to only one trading venue.²⁰ When investors split their order between the exchange and the trading platform, they trade-off the gain in the price impact against a possibly higher cost due to different trading fees. For given trading fees and a given total quantity of shares sold by investors, Q , the optimal fraction of volume executed on the trading platform is:

$$\beta^* = \frac{1}{2} + \frac{f_e - f_{pl}}{2RP^*Q} \quad (9)$$

If the trading fees are identical on both trading venues, investors execute half of their order on each trading venue. If trading fees differ, investors execute the larger part of their order on the cheaper trading venue. The higher the risk aversion of the market makers, λ , the larger the gain investors obtain from splitting their orders. Therefore, a higher λ makes investors less sensitive to the difference in trading fees and to changes in trading fees. If there is no price impact, $\lambda = 0$, there is no reason for investors to split their order. They trade on the trading venue with the lowest trading fee. Similarly, a high precision of public information reduces the price impact on both the exchange and the platform, and reduces the incentive of investors to split their order-flow. When information is perfectly revealed ($\theta = 1$), they also trade only on the cheapest venue.

The risk aversion parameter λ determines the strength of competition between the two trading venues. The smaller λ is, the tougher is competition in trading fees since the distribution of the volume across both trading venues is more sensitive to differences in trading fees. Investors gain less from splitting their orders. In contrast, a large λ stands for weak competition in trading fees because the incentive of investors to split their order is

²⁰ The possibility to reduce the price impact by splitting orders across several market makers (or markets) grounds also the models in Bernhardt and Hughson (1997) and Chowdry and Nanda (1991). However, utility gains from the possibility to trade on several venues can also stem from the possibility to avoid queuing in an order book and to increase the execution probability of a limit order (Foucault and Menkveld (2008)). Theoretical and empirical research displays mixed results concerning the existence of such gains. However, recent empirical work (O-Hara and Ye (2009), Foucault and Menkveld (2008)) find evidence consistent with the existence of liquidity gains associated to fragmentation.

strong. This parameter can be compared to the transportation cost in the Hotelling (1929) model in that it determines the degree of price competition between the two trading venues.

IPO. At the IPO stage, both investors anticipate that they might be either a liquidity trader or an informed trader in the future. Both investors face the price impact related to the risk aversion of market makers. They also anticipate that the liquidity trader trades at a loss against the other investor who is the informed trader. At this stage we make the assumption that becoming the informed trader or the liquidity trader is equally likely: $\gamma = 0.5$. The impact of informed trading on the main result will be developed at the end of the analysis. Regardless of whether investors trade, they anticipate to bear a fraction of the compliance costs and take this cost into account in the price they are willing to pay for the shares

In the case investors become the liquidity trader, they expect to keep their holding until the end of the game with probability $\frac{1}{2}$. Their expected wealth per share is:

$$E[V] - \frac{1}{2} \left(S + \frac{1}{4} \overline{RP} \alpha K + \bar{f} \right) - \frac{C(\theta)}{K} \quad (10)$$

where $\overline{RP} = \frac{\lambda}{2} \text{Var}[V|S] (\beta^{*2} + (1 - \beta^*)^2)$ is the weighted marginal risk premium of market makers and $\bar{f} = \beta^* f_{pl} + (1 - \beta^*) f_e$ is the weighted trading fee. In the case investors become the informed trader, they expect to trade with probability $1/2$. Their expected wealth per share is:

$$E[V] + \frac{1}{2} \left(S - \frac{1}{4} \overline{RP} \alpha K - \bar{f} \right) - \frac{C(\theta)}{K} \quad (11)$$

The owner of the firm sells the shares at the highest price he can obtain from the investors, i.e. the price which makes them indifferent between buying and not buying. Therefore, the IPO price corresponds to the expected per share wealth of investors before they know their type:

$$P_{IPO}^* = E[V] - \frac{1}{4} \overline{RP} \alpha K - \frac{1}{2} \bar{f} - \frac{C(\theta)}{K} \quad (12)$$

The IPO price increases when investors bear smaller trading costs. Since the probability to be a liquidity trader is $\frac{1}{2}$, the expected adverse selection cost is offset by the expected information gain and does not affect the IPO price. If the probability to become the liquidity trader was large, $\gamma > 0.5$, the adverse selection cost would reduce the IPO price and vice versa if $\gamma < 0.5$. The results derived in the analysis which follows hold for any probability γ . The impact of different value for this probability is explained in an extension.

The possibility to sell shares on the exchange allows the owner of the exchange to receive a payment which is certain and therefore to reduce his risk. However, the cost of selling shares consists in selling them below their expected value due to the trading costs borne by investors. Also, investors pass the compliance costs through to the owner. Thus, it is the owner of the firm who bears the full burden of the compliance with listing requirements.

Replacing the expression of the IPO price (equation 12) in the objective of the owner (equation 1), yields the optimal fraction of shares the owner is willing to sell on the exchange:

$$\alpha^* = \frac{2K\rho\sigma_v^2 - 0.25(f_e + f_{pl})}{K(2\rho\sigma_v^2 + 0.125RP)} \quad (13)$$

where $\sigma_v^2 = 0.25(x_h - x_l)^2$

The fraction, α^* , is always smaller than 1. The owner never sells his entire holding. We assume that K is large enough for α^* to be greater than zero. The owner sells more shares the smaller the trading costs of investors are since higher trading costs reduce the IPO price and therefore the proceeds from the sale. In particular an increase in the level of listing requirements reduces the price impact since the uncertainty about the final payoff becomes smaller, and leads to a higher α^* .

The fraction of shares sold by the owner depends on the unweighted average of the trading fees and on the price impact. It is independent of the actual distribution of the volume across the two trading venues determined by β^* . Thus, the number of issued shares is determined as if investors traded half of their shares on each market. This is because the gain obtained by investors due to the possibility to strategically allocate their order-flow across the two trading venues (compared to a situation in which they trade half of their order on each venue) leads to a utility increase for the owner which is independent of the quantity of traded shares, $(f_{pl} - f_e)^2 / 4RP$.

The surplus of the owner is obtained by combining equation 13 with the IPO price and his utility:

$$\Delta U(\alpha^*) = \frac{(2K\rho\sigma_V^2 - 0.25(f_e + f_{pl}))^2}{0.25RP + 4\rho\sigma_V^2} + \frac{(f_e - f_{pl})^2}{4RP} - \alpha^* C(\theta) \quad (14)$$

The surplus of the owner increases the smaller the trading costs of investors are because he sells more shares at a higher price. It increases also with a higher gain from the optimal volume allocation across the trading venues, represented by the second term in equation 14, because this gain increases furthermore the IPO price. Both elements of the owner's surplus increase with the level of listing requirements.

The initial owner lists his firm if and only if his surplus exceeds the compliance costs: $\Delta U(\alpha^*) > (1 - \alpha^*)C(\theta)$. Otherwise, the utility gain he obtains from diversification is not large enough to compensate the compliance costs related to the listing.²¹

Although producing public information at a later period about the value of the firm increases the surplus that the owner of the firm obtains at the IPO, he cannot credibly commit to produce this information when he keeps the control over the firm. Information is produced in stage 4, after the IPO, date at which the initial owner of the firm does not intervene on the market. At that stage, he does not benefit from revealing information but bears the cost. Thus, as long as he keeps the control over the firm ($\alpha^* < 0.5$) he will not release an informative signal ex post. This is in particular the case, when the risk aversion of the owner is small enough. The present analysis does not deal with voluntary information disclosure which is left for future research. It is assumed throughout the analysis that the firm does not disclose information voluntarily.²²

4. Listing and trading: the monopoly case

The analysis of the decisions on the trading fee and on the level of listing requirements is first carried out by considering a situation in which the exchange is a monopolist both in

²¹ The fact that costs related with the compliance of listing standards, in particular those concerning information disclosure and corporate governance, might exceed the benefits of a listing on a highly regulated exchange for some firms is debated in the literature on cross listings and in particular on the competitiveness of the NYSE. Anecdotal evidence also indicates the deterring role these costs can have for firms seeking to list.

²² The firm might not release information at stage 4 for other reasons: There might be an interest conflict between informed and uninformed shareholders (if these have the control) or a moral hazard problem between the shareholders and the manager of the firm.

listing and in trading. In this case, $\beta = 0$ by assumption. This allows a better understanding of the determinants of the optimal level of listing requirements as well as of the determinants of the trading fee. The next section includes the competing trading platform in the analysis.

The volume expected to occur in $t = 5$ is:

$$0.5\alpha^{**} K \quad (15)$$

where α^{**} is the fraction of shares sold by the owner in the case the exchange is a monopoly in trading.²³ The exchange knows that one among the two investors will become the liquidity trader and the other the speculative trader. Therefore, the probability with which investors expect to become the liquidity trader in $t = 3$, does not affect the volume that occurs once the type of investors has been realized. The liquidity trader trades with probability $\frac{1}{2}$ and the speculative trader trades if he has observed that the firm has a low value which occurs with probability $\frac{1}{2}$. Both investors sell their entire holding if they trade, $0.5\alpha^{**} K$.

The exchange determines its trading fee, $f_{e,m}$, to maximize its expected profit, $\Pi_{e,m}$. The profit is composed of the listing fee, F , and the total volume multiplied by the trading fee. The objective function of the exchange is:

$$\underset{f_{e,m}}{Max}\Pi = v(\Delta U(\alpha^{**}) - (1 - \alpha^{**})C(\theta)) + f_{e,m} 0.5\alpha^{**} K \quad (16)$$

The exchange determines the trading fee so as to maximize its income from trading and listing. The surplus of the owner contains the part of the compliance costs borne by investors. This cost has no influence on the trading fee determined by the exchange. At a given level of compliance costs, it corresponds to a fixed cost for the firm and thus for the exchange.

The trading fee has opposite effects on the exchange's profit: On the one hand it increases the income per traded share. However on the other hand, not only does it reduce the number of shares sold by the owner of the firm and therefore the trading volume, it also reduces the surplus and thereby the revenue from listings. The exchange determines the trading fee taking into account its negative effect on the volume as well as on the listing fee.

²³ $\alpha^{**} = \frac{2K\rho\sigma_v^2 - 0.5f_{e,m}}{K(2\rho\sigma_v^2 + 0.25RP)}$

Proposition 1

The optimal trading fee is: $f_{e,m}^* = 2K\rho\sigma_v^2 \left[1 - \frac{\nu}{2-\nu} \right]$ (17)

The equilibrium trading fee depends on the size of the volume and on its impact on the listing fee. The more the initial owner gains from selling shares (the higher his risk aversion is or the more risky the asset is), the higher is the volume on the exchange. This leads to a higher equilibrium trading fee. The equilibrium fee does not depend on the level of listing requirements. This is not only because informed trading does not affect the IPO price and thus the size of the IPO issue. This comes also from the fact that the marginal gain in the revenue from trading as well as the marginal loss due to a smaller amount of issued shares when the trading fee increases are both scaled by the price impact. A higher level of listing requirements reduces the price impact and contributes thereby to an increase in the marginal gain and in the marginal loss from a higher trading fee. For an equal quantity of shares, the exchange obtains a higher benefit per share, but the reduction in the number of issued shares is also larger. Both effects cancel out.

The exchange takes into account the negative effect of the trading fee on its listing fee, it therefore sets a trading fee that is smaller than the fee maximizing the revenue from volume. In equation 19, the expression $2K\rho\sigma_v^2$ represents the optimal trading fee if there is no revenue from listing. This expression is reduced by the term $2K\rho\sigma_v^2\nu/(2-\nu)$ which represents the negative effect of a higher trading fee on the profit of the exchange through the reduced listing fee.

Because of this interdependence between listing and trading fees, investors pay a lower trading fee and are better off (for a given level of listing requirements) if the exchange exercises both functions, listing and trading, than if the exchange only organizes trading. As a consequence, the volume on the exchange and the surplus of the owner are larger when both functions are exercised by the same institution, the exchange, than when these functions are disconnected and fulfilled by two independent institutions.

In the present case, the optimal trading fee is always positive. This is due to the assumption that the probability with which one investor observes private information is 1 and that the probability of becoming a liquidity trader is $\frac{1}{2}$. If these assumptions are relaxed, the equilibrium trading fee could also be negative for some parameter regions. Extending the model in such a way allows for situations in which the exchange pays for order-flow because it has income from listing.

The owner of the firm undertakes the IPO if and only if its utility gain net of all costs is greater than zero:

$$\left[\frac{(2K\rho\sigma^2)^2}{(RP+4\rho\sigma^2)(\nu-2)^2} - C(\theta) \right] (1-\nu) \geq 0 \quad (18)$$

The exchange sets the equilibrium level of listing requirements such as to equalize its marginal gains that stem from a higher number of issued shares and a higher utility gain of the owner of the firm, to the marginal losses stemming from the increased compliance costs that reduce the revenue from listing. However, there is an upper bound to the level of listing requirements given by the participation constraint of the firm (equation 18). The exchange never sets the level of listing standards above the level rendering the participation constraint of the owner binding.

5. Competition for volume.

The existence of the alternative trading platform allows investors to benefit from a smaller total price impact because they can trade on both venues (or equivalently with two market makers) rather than on a single one. This reduces the trading costs and thus the cost borne by the owner of the firm when he lists his firm and sells shares. The number of issued shares and consequently the overall trading volume are higher in the case in which the alternative platform exists. This also leads to a higher surplus earned by the owner and thus to a higher income from listing for the exchange.

The smaller price impact faced by investors also increases the sensitivity of the volume and of the owner's surplus to changes in trading fees. Since the owner of the firm issues more shares due to the smaller price impact, the effect of higher trading fees per traded share affects his utility to a larger extent. When trading fees increase, he will reduce the number of shares he issues to a larger extent than in the monopoly case.

When the exchange and the trading platform determine their trading fees, they take into account how changes in trading fees affect their income per shares as well as their market share on trading volume. As in the benchmark case, trading fees affect the volume and the surplus of the owner. However, trade-offs are finer than previously because the two trading venues depend on each other: a change in the trading fee on one trading venue alters the volume and the revenue of the other trading venue. If, for instance, the trading platform

lowers its trading fee, the overall number of shares in the economy becomes larger. The platform benefits not only from a higher fraction of the volume, but this fraction concerns an overall larger number of shares. In this case, the exchange has a smaller fraction of the volume but the general increase in the number of shares limits the loss of revenue incurred by the exchange in its trading activity. Furthermore, the exchange benefits from a higher listing fee since the surplus of the initial owner of the firm is larger.

While in the monopoly case, the trading fee was only determined by its impact on the total volume, trading fees in the case of competition depend also on the degree of competition for trading volume between the trading venues. Strong competition for trading volume corresponds to a situation in which the market shares of the trading venues are highly sensitive to changes in trading fees (see equation 9).

The expected overall volume is determined as in section 2 (equation 15). The exchange and the platform set the trading fee simultaneously to maximize their expected profits:

$$\Pi_e = v(\Delta U(\alpha^*) - (1 - \alpha^*)C(\theta)) + f_e(1 - \beta^*)\alpha^*K \quad (19)$$

$$\Pi_{pl} = f_{pl}\beta^*\alpha^*K \quad (20)$$

While the adjustment of trading fees affects only the distribution and size of the volume from the platform's point of view, it also affects the listing fee of the exchange. The equilibrium trading fee set by the exchange differs from the fee set by the platform because the exchange takes into account the negative effect of the average trading fee on its income from listing.

Proposition 2

- (i) If $\lambda > 0$, the exchange always sets a smaller trading fee than the trading platform in equilibrium: $f_e^* < f_{pl}^*$.
- (ii) If $\lambda = 0$, $f_e^* = f_{pl}^* = 0$ and investors are indifferent between trading on the exchange and trading on the trading platform.
- (iii) For $\lambda < \bar{\lambda}_0$, the average trading fee is smaller than the trading fee in the monopoly case. For $\lambda > \bar{\lambda}_0$, the average trading fee is higher.

The determination of the threshold $\bar{\lambda}_0$ is explained in the appendix.

In the case, in which fragmentation does not lead to gains for investors, e.g. when $\lambda = 0$, they trade on the trading venue with the lowest trading fee. There is no other

reason for investors to split their order. This leads to price competition à la Bertrand and eventually to zero trading fees on both trading venues.

If $\lambda > 0$, the exchange and the platform capture a fraction of the order flow since investors prefer to split their orders between the two trading venues rather than to execute their order on only one trading venue. This relaxes price competition and leads to positive trading fees. The income which the exchange earns from listing, increases the smaller the average trading fee is, since this leads to a higher surplus of the owner. Thus, the exchange has an incentive to trigger price competition by setting a smaller trading fee than the trading platform. Here again, the existence of a income from listing makes investors and thus the owner better off (everything else equal) since it leads to overall lower trading fees than when this income did not exist.

When the gain from fragmentation is small, investors are sensitive to differences in trading fees. In this case, both trading venues are induced to set a small trading fee. The exchange as well as the platform increase their trading fees when the gain related to fragmentation becomes large (when λ becomes large). In this case, a large difference in trading fees has a minor impact on the distribution of the trading volume. The average trading fee faced by investors can even exceed the equilibrium trading fee set by a monopolist. This is because the trading platform is induced to increase its own trading fee above the monopoly level when the trading volume is not sensitive to the difference of trading fees. It increases thereby its revenue from trading without losing much trading volume.

Lemma 1

For a given level of listing requirements:

- (i) The overall volume is larger than in the monopoly case
- (ii) The utility gain that the owner obtains from the IPO is larger than in the monopoly case
- (iii) The exchange obtains a higher profit if and only if $\lambda > \bar{\lambda}_1$. Otherwise, its profit is smaller.

The possibility of multi-market trading increases the utility gain of the owner and the number of shares he sells in equilibrium because he obtains two gains from this possibility: either the average trading fee is larger but the owner benefits from the increased absorption capacity of the markets which is reflected in the smaller total price impact, or the markets are anyway able to absorb large volumes but the induced competition leads to smaller trading fees. In any case, the total trading costs of investors are lower than in the monopoly situation. While the total volume is larger with fragmentation, the part of the volume captured by the

exchange is smaller than in the monopoly case. Despite the loss of volume, the exchange can obtain a higher profit in the presence of an alternative platform when competition on trading fees is weak enough to compensate the loss in revenue due to a smaller trading volume. The higher income from listing is not sufficient for the exchange to obtain a larger profit; it must be complemented by a high enough revenue from trading.

This discussion shows that there might be conflicting interests regarding competition for trading volume between the firm and the exchange. While the owner of the firm always benefits from competition (at a given level of listing requirements), the exchange only benefits from it when the pressure on trading fees is low enough.

Not only does competition for volume change the level of listing fees, the surplus from the IPO and the profit of the exchange, it also affects the sensitivity of these variables to changes in the level of listing requirements.

Lemma 2

- (i) Equilibrium trading fees diminish with the level of listing requirements.
- (ii) The larger the gain from fragmentation is (the larger λ is), the less equilibrium trading fees are sensitive to changes in the level of listing requirements.

In contrast to the monopoly case, the trading fee set by the exchange is sensitive to changes in the level of listing requirements. A more informative signal has two opposite effects. First, it reduces the price impact on both trading venues and thereby the gain that investors obtain from fragmentation. This lowers their incentive to split their orders across the two trading venues and enhances the pressure on trading fees, which leads to smaller trading fees in equilibrium. Second, a higher level of listing requirements increases the gain per share the exchange obtains from increasing its trading fee but enhances also the marginal loss due to a smaller trading volume. Not only do the lower trading costs induce the owner of the firm to issue more shares, they also render the market share of the exchange more sensitive to the difference in the trading fee.

If the gain of investors coming from multi-market trading is small (if λ is small), the competition effect dominates the volume effect and leads to a sharp decrease in equilibrium trading fees when the level of listing requirements increases. If, in contrast, the gain from fragmentation is large (if λ is large), the volume effect gains in importance and nearly offsets the competition effect, which is then weaker. The equilibrium trading fees become nearly insensitive to changes in the precision of public information.

Lemma 3

The total trading volume and the income from listing increase more with the level of listing requirements when an alternative trading platform exists, compared to a situation in which the exchange is a monopolist in trading.

The total trading volume becomes more sensitive to changes in the level of listing requirements because it reacts more to changes in trading costs as compared to the monopoly case. This amplifies in particular the positive effect of a reduction in the trading fee on the trading volume when public information becomes more precise. Since the sensitivity of the volume to changes in the level of listing requirements increases, the surplus of the initial owner of the firm also increases more in equilibrium. A higher level of listing requirements contributes therefore also to an increase in the revenue from listing.

The exchange benefits from the increase in the total volume because its market share also increases when public information becomes more precise. Although both trading fees diminish with θ , the trading volume becomes more sensitive to the difference in trading fees which yields a higher market share to the exchange.

Lemma 4

For $\lambda < \bar{\lambda}_2$, the revenue from volume of the exchange diminishes with the level of listing requirements. For $\lambda > \bar{\lambda}_2$, it increases.

The revenue the exchange obtains from trading is affected in opposite ways when θ increases. First, the market share of the exchange becomes larger and this increase is the highest when competition on trading fees is low, i.e. when λ is small. Second the trading fee decreases and this in particular when λ is small either. The effect on the revenue from trading stemming from the evolution of the trading fee dominates the one related to changes in the market share. When competition is strong, the revenue from trading diminishes with the level of listing requirements due to the decreasing trading fee. When competition is weak, the revenue from trading increases with the level of listing requirements, due to the larger market share and to the negligible change in the trading fee. This contrasts to the monopoly case, in which the revenue from trading always increases with the level of listing requirements since the exchange captures the entire growth in the trading volume.

Even though the exchange might be able to increase its revenue from trading by setting a higher signal precision, this increase is always smaller than when the exchange is a monopolist. Thus, even with weak competition and despite the positive effects that competition has on the overall trading volume and on the exchange's market share, the

exchange is not able to improve its revenue from trading to the same extent than when it is a monopolist. Weak competition only limits the loss the exchange suffers compared to the monopoly situation.

Proposition 3

Assuming that the participation constraint of the owner of the firm is not binding:

- (i) If $\lambda > \bar{\lambda}_3$, the exchange sets a higher level of listing requirements than in the monopoly case.
- (ii) If $\lambda < \bar{\lambda}_3$, the exchange sets a smaller level of listing requirements than in the monopoly case.

The determination of the threshold $\bar{\lambda}_3$ is explained in the appendix.

If the gain from fragmentation is large, an increase in the signal precision limits competition on trading fees. If the exchange raises its level of listing requirements, it benefits not only from a higher increase of the revenue from listing compared to the monopoly case. The increase in the revenue from trading is smaller than in the monopoly case, but this difference is limited by the possibility for the exchange to raise its market share. The large gain due to the possibility to split orders combined with the low competitive pressure allows the exchange to benefit more from an increase in listing requirements than when the exchange is a monopolist. As a consequence, the exchange sets a higher level of listing requirements in equilibrium.

If the gain from fragmentation is small, competition is strong leading to a sharp reduction of the trading fee when the signal precision increases. Although the decrease in the trading fee associated with a higher signal precision contributes to an even higher increase in the surplus of the owner, and thus in the revenue from listing, this is not sufficient to compensate the loss in revenue from trading. In this case, the exchange benefits less from an increase in the signal precision than when it were a monopolist and sets therefore a smaller level of listing requirements.

When the exchange faces competition in volume, it might determine either a higher or a smaller level of listing requirements in equilibrium, compared to the case in which the exchange is a monopoly in trading. As a consequence, competition in volume does not necessarily lead to a “race to the bottom” in terms of listing requirements. The determinant factor for this decision is the gain investors obtain from fragmentation which determines the strength of price competition and thereby the sensitivity of the profit of the exchange to changes in listing requirements.

The fact that the exchange might raise its level of listing standards in the presence of a competing trading platform stems from two effects related to multi-market trading. First, it lowers the trading costs of investors which translates into a higher value of shares and a higher number of shares on the market. Second, competition on trading fees might be limited if the absorption capacity of the markets is improved by the existence of the alternative trading venue.

Welfare effects of fragmentation. The existence of two trading venues procures three types of welfare gains to investors. First, they gain from the possibility to fragment their order and to thereby reduce their trading costs. In the present setting, the gain from fragmentation stems from the risk aversion of the liquidity suppliers and from the assumption that the entry of the alternative trading venue is equivalent to the entry of an additional market maker. The idea, that multi market trading improves the liquidity of shares is debated in the literature but is consistent with recent empirical work by Foucault and Menkveld (2008) and O'Hara and Ye (2009) as well as studies on exchange traded funds (Boehmer and Boehmer (2003)). While this analysis claims that there is a link between the motivation of multi-market trading and the trade-offs faced by a profit maximizing stock exchange deciding over listing requirements, it does not claim that gains from fragmentation must come from the mechanisms modeled here. The results of the present analysis should also hold in a setting in which the additional trading venue enhances competition among liquidity suppliers or increases the probability of trading, which would be consistent with the theory part of Foucault and Menkveld (2008).

The second welfare gain for investors is the competition in trading fees induced by the fragmentation of orders. The intensity of competition on trading fees is inversely related to their gains from fragmentation. Thus, when the gain from fragmentation is small, investors benefit from the presence of several trading venues through the small trading fees. If the liquidity gain related to fragmentation is large, the average trading fee paid by investors might be higher than without multi-market trading, but the net effect of competition is a reduction in their trading costs.

Third, investors might benefit from a higher level of listing requirements if the gain from fragmentation is large enough. This lowers even more their trading costs compared to the monopoly case. Most of the literature on multi market trading and order-low fragmentation takes the stock markets as given institutions and analyses the behavior of investors. The present analysis shows that multi-market trading affects also the decisions of trading venues and thereby the trading costs of investors (and the cost of capital of firms).

6. Extensions

Social optimality. The last section has stated that investors benefit from multi-market trading because their trading costs diminish. The exchange, however, is not always in favor of competition, in particular when the pressure on trading fees is strong. The firm issuing shares also bears the costs related to the listing requirements. Competition is only socially beneficial if these social costs are compensated by the social gains.

Proposition 4

Competition is socially preferable to a monopoly exchange if:

- (i) $\theta_{monop}^* = \theta_{comp}^*$
- (ii) $\lambda < \bar{\lambda}_4$ and $\theta_{monop}^* > \theta_{comp}^*$
- (iii) $\lambda < \bar{\lambda}_5$, $\theta_{monop}^* < \theta_{comp}^*$

When the level of listing requirements is the same with and without competition, the costs related to the listing requirements are the same. The social gains, composed of the net surplus of the initial owner of the firm and the revenues of the exchange and the platform, are larger due to the smaller trading costs borne by investors. Therefore, competition is always socially optimal in this situation.

If, with competition, the equilibrium level of listing requirements is smaller than in the monopoly case, the positive welfare effects of fragmentation are reduced which lowers the social gains related to fragmentation. If on the same time, competition on trading fees is strong enough, the smaller trading fees paid by investors in the case of competition compensate the losses due to the lower level of listing requirements. In this case, social welfare is also improved with competition. The threshold on the strength of competition, $\bar{\lambda}_4$, depends on the steepness of the cost function. The smaller θ_{monop}^* is and the flatter the cost function is, the lower is also this threshold.

If the level of listing requirements is higher with competition than without, the existence of the alternative platform is only socially beneficial if competition is not too weak. However, the threshold in this case is larger than in part (ii) of proposition 4 - $\bar{\lambda}_5 > \bar{\lambda}_4$. It is also larger than the threshold at which the exchange begins to regulate listing more strictly with competition - $\bar{\lambda}_5 > \bar{\lambda}_3$. A large λ allows investors to reduce their price impact, but at the same time it leads to average trading fees that are larger than the monopoly fee. This limits the gain investors obtain from fragmentation and thereby its positive welfare effects compared

to the monopoly situation. This situation implies also higher compliance costs borne by firms which reduces the exchange's profit and limits the social desirability of competition.

As a conclusion, regardless of whether competition leads to more or less regulation of listings by the exchange, it is only socially desirable when the pressure on trading fees is strong enough.

Sub-optimal regulation. More precise public information does not only procure a gain to the exchange, it also increases the revenue of the trading platform (as long as θ is not too large or λ very small) and the utility as well as the costs of the initial owner of the firm. However, the exchange takes the decision over θ considering only its own profit and not the gains or losses of the trading platform and of the owner.

Proposition 5

The level of listing requirements the exchange sets in equilibrium is sub-optimal from a social point of view, regardless of whether there is competition in volume or not.

A social planner would set the level of listing requirements taking into account the profit of the trading platform in addition to the surplus of the owner. The socially optimal signal precision satisfies the following condition:

$$\frac{\partial \Pi_e}{\partial \theta} + \frac{\partial \Pi_{pl}}{\partial \theta} + \frac{\partial (\Delta U - C(\theta))}{\partial \theta} (1 - \nu) = 0 \quad (21)$$

Listing requirements procure different gains and costs to investors and to the exchange. If the exchange determines the listing requirements, it does in particular not internalize the utility gain and the additional compliance costs borne by the owner of the firm associated with higher listing requirements. This induces the exchange not to set a socially optimal level of listing requirements. This problem is analyzed empirically by Macey et al. (2005) in the context of delisting decisions. The authors show that delisting decisions are taken in a way that harms investors but that seems to procure gains to the NYSE. They interpret the evidence as indicating that the NYSE does not internalize the loss of utility of investors in its delisting decisions.

In the case of competition, the exchange also fails to internalize the profit of the trading platform in its decision on listing requirements. This enhances the sub-optimality of listing requirements when they are determined by the exchange, regardless of whether

competition induces the exchange to raise or to lower listing requirements compared to the monopoly case. Thus enhanced under-regulation due to competition in order-flow does not necessarily imply a smaller level of listing requirements.

One possibility to partially solve the problem related to the public good nature of listing requirements would consist in merging both trading venues. In this case, the trading fees and the listing requirements maximise the joint surplus of both organisations. Since investors benefit from fragmentation, the merged exchange has an interest to keep two distinct trading platforms. However, the merged exchange does not have to compete for volume, but it can determine the trading fees on both platforms such that the distribution of volume is optimal for the merged exchange.

Proposition 6

If the trading platform and the exchange are merged to constitute one integrated organisation:

- (i) The trading fees on both trading venues are identical to the fee set by a monopoly exchange.
- (ii) When $\lambda > 0$, the profit of the merged entity is larger than in the monopoly case.
- (iii) The level of listing requirements set by the integrated organisation is higher than in the monopoly case if and only if $\lambda > \bar{\lambda}_g$. It is smaller if $\lambda < \bar{\lambda}_g$.

The determination of the threshold $\bar{\lambda}_g$ is explained in the appendix.

The merged organisation benefits from the gain of fragmentation and from the absence of competition. This explains the higher profit of the merged entity compared to the monopoly case. To maximise the gain from fragmentation, the merged entity sets the same trading fee on both venues, so that the volume is equally distributed. Since the merged entity determines the trading fees only relative to their effects on the number of issued shares and on the total trading volume, it faces the same trade-off than the monopoly exchange (with only one trading venue). In particular, marginal losses and marginal gains related to an increase in the trading fee are scaled by the price impact. Therefore, the price impact does not determine the optimal trading fee which is the same as in proposition 1.

The gain that the merged entity obtains when it increases the signal precision, however, might still be lower than when the exchange is a monopolist. Although a smaller price impact renders the profit of the exchange more sensitive to changes in the level of listing requirements, the price impact changes less in the case of the merged entity when θ increases. When λ is small, the increase in the revenue when public information becomes more precise is smaller for the merged entity and the equilibrium level of listing requirements is then also smaller. When λ becomes large, the revenue of the merged entity increase more

with the signal precision as compared to the monopoly situation. This leads to a higher level of listing requirements in equilibrium.

The merged entity sets the same trading fee than the monopolist exchange with only one trading venue. Whether it is socially desirable depends on two factors. First, if the equilibrium level of listing requirements is smaller than in the monopoly case, it depends on whether this offsets the gains of investors related to the possibility to fragment their orders. Second, if the equilibrium level of listing requirements is above the one prevailing in the monopoly case, it depends on whether the additional costs imposed on the firm are offset by the additional gains.

The merged entity might also be socially preferable to competition between the exchange and the platform. The merged entity obtains a higher marginal revenue from listing requirements than the exchange when there is competition. Indeed, the merged entity benefits from the increase of the total volume and does not lower its trading fee. Despite the possibly higher level of trading fees, the merger of the exchange and the platform might improve social welfare if it leads to a sufficiently higher equilibrium level of listing requirements without increasing the costs too much.

Informed trading. The analysis has, up to this point, assumed that the probability to become the liquidity trader is $\gamma = 0.5$. This has allowed abstracting from the part of the spread that emerges due to possible informed trading on the secondary market. The adverse selection costs anticipated in the case of a liquidity shock were offset by the information gain anticipated in the case private information is observed. When this hypothesis is relaxed, investors discount (increase) the IPO price they are willing to pay for the shares issued by the initial owner of the firm by an additional component reflecting the expected loss (or gain) related to informed trading:

$$P_{IPO}^* = E[V] - (2\gamma - 0.5)S - \frac{1}{4} \frac{\overline{RP\alpha K}}{K} - \frac{1}{2} \bar{f} - \frac{C(\theta)}{K} \quad (22)$$

When $\gamma > 0.5$, it is more likely to become the liquidity trader and thus, the adverse selection cost gains in importance for investors. The IPO price is discounted by the information component of the spread, S . This additional expected trading cost also reduces the number of issued shares, the surplus of the initial owner of the firm, the equilibrium trading fee and the profit of the exchange and of the trading platform. If, on the contrary, observing private

information is more likely ($\gamma < 0.5$), the information component, is an expected gain and raises the IPO price. This increases all the aforementioned variables.

The probability, γ , affects the objective function of the exchange in opposite ways depending on its value. It influences therefore also the decision on the level of listing requirements. An increase in the precision of public information lowers S . Thus it affects the profit of the exchange not only through the price impact but also through the information component of the spread. If $\gamma > 0.5$, the threshold up from which the exchange facing competition from a platform regulates listing more strictly than in the monopoly case is lower than in proposition 3. This is because in addition to reducing the price impact, a higher level of listing requirements also reduces the information component of the spread. Since investors are more sensitive to changes in trading costs when an alternative trading platform exists, the exchange obtains an additional gain from regulation compared to the monopoly case. If $\gamma < 0.5$, the threshold is higher because increasing θ lowers the expected information gain of investors. Consequently, the characteristics of the investor base present on an exchange and, in particular, its access to private information has an impact on the way in which more public information influences the price of shares and thereby the decisions of the firms and eventually those of the exchange.

7. Conclusion

The present model aims at analyzing the relationships between listing requirements, the organization of trading and the disparities between social and private optima regarding listing requirements. It has shown that competition in volume has an impact on the level of listing requirements set by an exchange but this impact is not necessarily detrimental to investors, although it might enhance under-regulation with respect to the social optimum. Also, competition in volume does not necessarily induce the exchange to lower its level of listing requirements despite the regulatory costs borne partially by the exchange and the loss of market share in volume. This is in particular the case, when the possibility to fragment orders yields important gains to investors.

The main result of the model is that the effect of competition in volume on the regulatory activity of a self-regulating, profit maximizing exchange regarding listings depends on the nature of the competition for order-flow. If competition is mainly driven by prices, a profit maximizing exchange is induced to lower its level of listing requirements. If

competition is mainly driven by gains related to the fragmentation of orders, the exchange can benefit from positive welfare effects and is induced to raise its level of listing requirements

This model yields important policy implications. It shows that the question whether an exchange should be self-regulating with respect to listings in general is highly complex and debatable. Listing requirements are a public good. If an exchange privately determines listing requirements, it does not internalize the utility of investors (which is the case with and without competition in volume) nor does it internalize the gains of additional trading venues.

In the case where several trading venues exist, a merger of the trading venues with the exchange might reduce the inefficiency of listing requirements since the merged organization maximizes the joint surplus. However, the merged organization only benefits from listing requirements if the gain which investors obtain from the fragmentation of orders is sufficiently large. Thus, it is again the nature of fragmentation that determines whether the merger of trading venues leads to less regulation or not.

This analysis shows that there is an interdependence between the listing fee and the trading fees when the listing fee is proportional to the surplus of the owner of the firm. The association of these two activities in one single profit maximizing entity contributes to the reduction of the overall level of trading fees. Thus, combining the functions of listing and trading in one entity improves the welfare of investors. This point holds as long as the revenue from listing depends on transaction costs on the exchange as well as on competing trading venues.

In the current policy debate around how listing and trading should be organized, given that there are trading platforms that compete with exchanges for order-flow in shares of the firms listed on the exchange, it is generally stipulated, that since listing regulation is a public good, it is under-provided by a profit maximizing exchange in the presence of order-flow fragmentation. Listing should therefore be separated from the trading activity. The present paper complements this debate by two elements. First, it has demonstrated that under-provision of regulation exists even without competition in volume . Second, it has shown that this debate should take into account the impacts of possible welfare effects on the decision of the exchange: There can be positive welfare effects in the case of competition in volume, but there can also be negative welfare effects when listing is separated from trading.

The present analysis could be extended in several ways to better understand the causes and consequences of the transformations occurring in the stock market industry. The listing decision of firms and the entry decision of investors could be determined endogenously. In particular, if competition in volume leads to lower trading fees, it could attract a higher

number of firms and of investors into the market. This could lead to a higher liquidity on all trading venues as well as to better risk sharing opportunities for investors and consequently to a lower cost of capital for firms (Pagano 1989a, 1989b, 1993). These effects could enforce the positive impact of competition on the welfare of investors and could eventually lead to a higher level of listing requirements if it is determined by the exchange.

On the empirical side, only a few papers compare institutional characteristics across exchanges in the world. Frost et al. (2006) find evidence for a positive link between the strictness of disclosure standards as well as the quality of enforcement and the liquidity on exchanges. Clayton et al. (2006) establish a link between the choice of trading mechanisms and institutional characteristics of the home countries of exchanges such as the legal system. The theory developed in this paper calls for an extensions of this literature, and in particular for an analysis of competition in volume in relation with the price structure as well as the regulatory competency of stock markets.

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Appendix

Appendix A1

In the case of a good signal ($s = x_h$), the bid price the liquidity trader expects is: $P_B \theta + (1 - \theta)x_l$, where P_B is determined in equation 7. In the case of a bad signal ($s = x_l$), the bid price the liquidity trader expects is: $P_B(1 - \theta) + \theta x_l$. Since, before $t = 4$, the signals are expected to occur with probability $\frac{1}{2}$, the equally weighted average of the expected bid prices conditional on public information yields equation 8.

Proposition 1

The profit function of the exchange is concave in the trading fee. When the expression for α^{**} is replaced in the objective function (equation 18), it follows that $\frac{\partial^2 \Pi_{e,m}}{\partial^2 f_{e,m}} < 0$. The optimal

trading fee when the exchange derives revenue from the listing activity is:

$$f_{e,m}^* = 2K\rho\sigma_V^2 \left[1 - \frac{\nu}{2 - \nu} \right]$$

If the exchange derives revenue only from the trading activity, the trading maximising this revenue is: $2K\rho\sigma_V^2$. Since $1 - \frac{\nu}{2 - \nu}$ is positive, the optimal trading fee is always smaller when the exchange has income from listing.

Proposition 2

(i) The maximisation of equations 21 and 22 yields optimal trading fees:

$$f_e^* = 2K\rho\sigma_V^2 * RP * A_e \text{ and } f_{pl}^* = 2K\rho\sigma_V^2 * RP * A_{pl} \text{ with } A_e < A_{pl}. \text{ Therefore}$$

$$f_e^* \leq f_{pl}^*.$$

The second derivatives of both profit functions are negative, $\frac{\partial^2 \Pi_e}{\partial^2 f_e} < 0$ and $\frac{\partial^2 \Pi_{pl}}{\partial^2 f_{pl}} < 0$, and the calculated optima are maxima.

(ii) It follows from (i) that $f_e^* = f_{pl}^* = 0$ if $\lambda = 0$ since in this case, $RP = 0$.

(iii) The weighted average trading fee in the case of competition is larger than the equilibrium trading in the monopoly case when the risk aversion of the market makers is large enough: $\lambda > \bar{\lambda}_0 \Rightarrow (1 - \beta^*)f_e^* + \beta^* f_{pl}^* > f_{e,m}^*$. Otherwise, the average fee is smaller: $\lambda < \bar{\lambda}_0 \Rightarrow (1 - \beta^*)f_e^* + \beta^* f_{pl}^* < f_{e,m}^*$. The threshold $\bar{\lambda}_0$ is such that $(1 - \beta^*)f_e^* + \beta^* f_{pl}^* = f_{e,m}^*$.

Lemma 1

Assume a level of listing requirements, θ

- (i) The volume in the monopoly and in the competition situations are determined by the fraction sold by the owner. In the case the exchange is a monopolist in trading, this fraction is smaller than when there is competition:

$$\alpha^{**} = \frac{4\rho\sigma^2}{(RP+4\rho\sigma^2)(2-x)} < \frac{2\rho\sigma^2(RP+4\rho\sigma^2)(RP(4+x)+8\rho\sigma^2(-3+x))}{(RP+8\rho\sigma^2)(8(\rho\sigma^2)^2(-3+x)+RP^2(-2+x)+8RP\rho P^2(-2+x))} = \alpha^*$$

- (ii) The surplus of the owner is larger with competition:

$$U(\alpha^{**}) = \frac{(2K\rho\sigma^2)^2}{(RP+4\rho\sigma^2)(2-x)^2} < \frac{(K\rho\sigma^2)^2(RP+4\rho\sigma^2)^2(32(\rho\sigma^2)^2(-3+x)^2+RP^2(8+(-4+x)x)+4RP\rho P^2(24+x(-14+3x)))}{(RP+8\rho\sigma^2)(8(\rho\sigma^2)^2(-3+x)+RP^2(-2+x)+8RP\rho\sigma^2(-2+x))^2} = U(\alpha^*)$$

- (iii) The exchange's profit is smaller than in the monopoly case if and if the risk aversion of market makers is small enough: $\lambda > \bar{\lambda}_1 \Rightarrow \frac{(2K\rho\sigma^2)^2}{(RP+4\rho\sigma^2)(2-x)} < \Pi_{comp}(\alpha^*, f^*)$.

Otherwise, the profit is larger with competition. The threshold $\bar{\lambda}_1$ is such that

$$\frac{(2K\rho\sigma^2)^2}{(RP+4\rho\sigma^2)(2-x)} = \Pi_{comp}(\alpha^*, f^*)$$

Lemma 2

In the parameter regions as they are specified in the model, the equilibrium trading fees

always decrease with the level of listing requirements: $\frac{\partial f_e^*}{\partial \theta} > 0$ and $\frac{\partial f_{pl}^*}{\partial \theta} > 0$. Furthermore:

$$\lim_{\lambda \rightarrow +\infty} \frac{\partial f_{pl}^*}{\partial \theta} \text{ and } \lim_{\lambda \rightarrow +\infty} \frac{\partial f_e^*}{\partial \theta}.$$

Lemma 3

$$\frac{\partial \alpha^{**}}{\partial \theta} < \frac{\partial \alpha^*}{\partial \theta} \text{ and } \frac{\partial U(\alpha^{**})}{\partial \theta} < \frac{\partial U(\alpha^*)}{\partial \theta}$$

Lemma 4

The revenue the exchange obtains from volume when it faces competition is:

$$RVol = \frac{8RP(K\rho\sigma^2)^2(RP+4\rho\sigma^2)(RP+6\rho\sigma^2)^2(1-x)}{(RP+8\rho\sigma^2)(8(\rho\sigma^2)^2(-3+x)+RP^2(-2+x)+8RP\rho\sigma^2(-2+x))^2}$$

$\lambda < \bar{\lambda}_2 \Rightarrow \frac{\partial RVol}{\partial \theta} < 0$. Otherwise $\frac{\partial RVol}{\partial \theta} > 0$. The threshold $\bar{\lambda}_2$ is determined such that $\frac{\partial RVol}{\partial \theta} = 0$.

Proposition 3

There is a threshold, $\bar{\lambda}_3$ at which $\frac{\partial \Pi_e(f_e^*, f_{pl}^*)}{\partial \theta} = \frac{\partial \Pi(f_{e,m}^*)}{\partial \theta}$.

If $\lambda > \bar{\lambda}_3$, $\frac{\partial \Pi_e(f_e^*, f_{pl}^*)}{\partial \theta} > \frac{\partial \Pi(f_{e,m}^*)}{\partial \theta}$. θ_e^* is always larger than the signal precision maximising the profit in the monopoly case.

If $\lambda < \bar{\lambda}_3$, $\frac{\partial \Pi_e(f_e^*, f_{pl}^*)}{\partial \theta} < \frac{\partial \Pi(f_{e,m}^*)}{\partial \theta}$. θ_e^* is always smaller than the signal precision maximising the profit in the monopoly case.

Proposition 4

- (i) For a given value θ , the cost generated by this level of listing requirements is the same in any cases. The sum of social gains is larger in the case of competition than in the monopoly situation: $U(\alpha^*) + Rvol_e(f_e^*) + \Pi_{pl}(f_{pl}^*) > U(\alpha^{**}) + Rvol_{e,m}(f_{e,m}^*)$. It follows that competition is socially preferable to the monopoly situation when the level of listing requirements remains identical.
- (ii) When $\theta_{monop}^* > \theta_{comp}^*$, competition improves social welfare if and only if: $U(\alpha^*) + Rvol_e(f_e^*) + \Pi_{pl}(f_{pl}^*) - C(\theta_{comp}^*) > U(\alpha^{**}) + Rvol_{e,m}(f_{e,m}^*) - C(\theta_{monop}^*)$ which holds only for $\lambda < \bar{\lambda}_4$.
- (iii) When $\theta_{monop}^* < \theta_{comp}^*$, competition improves social welfare if and only if: $U(\alpha^*) + Rvol_e(f_e^*) + \Pi_{pl}(f_{pl}^*) - C(\theta_{comp}^*) > U(\alpha^{**}) + Rvol_{e,m}(f_{e,m}^*) - C(\theta_{monop}^*)$ which holds only for $\lambda < \bar{\lambda}_5$.

Proposition 5

Case1: the exchange is a monopolist:

The socially optimal level of listing requirements is determined by the following equation:

$\frac{\partial \Pi_{e,m}}{\partial \theta} + \frac{\partial \Delta U}{\partial \theta} = 0$. Since $\frac{\partial \Pi_{e,m}}{\partial \theta}$ contains only a fraction of the compliance costs and the surplus of the owner is not internalized, the exchange sets a non-optimal level of listing requirements from a social point of view.

Case2: competition in volume

The socially optimal precision is determined by equation 23. The social optimum increases compared to the monopoly case by the extra term $\frac{\partial \Pi_{pl}}{\partial \theta}$. The difference between the socially

optimal signal precision and θ_e^* is determined by $\frac{\partial \Pi_{pl}}{\partial \theta} + \frac{\partial \Delta U}{\partial \theta}$. If $\frac{\partial \Pi_{pl}}{\partial \theta} + \frac{\partial \Delta U}{\partial \theta} < 0$, the social optimum is below the optimum of the exchange and the exchange over-regulates from a social point of view. If $\frac{\partial \Pi_{pl}}{\partial \theta} + \frac{\partial \Delta U}{\partial \theta} > 0$, the social optimum is above the optimum of the exchange and the exchange under-regulates from a social point of view.

Proposition 6

- (i) The merged exchange determines simultaneously the trading fees of both platforms by maximising the joint profit: $\underset{f_e, f_{pl}}{Max} \Pi_e + \Pi_{pl}$. The second derivatives of the joint profit with respect to either trading fees are negative. Thus the profit is concave in trading fees and the optimal trading fees are: $f_e^* = f_{pl}^* = f_{e,m}^*$.
- (ii) For $\lambda = 0$, the trading volume and the revenue from listing of the merged entity is identical to the one in the monopoly case with only one trading venue. Since the trading fee is the same as in the monopoly case, the profit of the merged entity is identical to the one in the monopoly case. If $\lambda > 0$, the trading volume and the revenue from listing are higher due to the gain from fragmentation. It follows that the profit of the merged entity is also higher than in the monopoly case.
- (iii) Denote the profit of the merged exchange by $\Pi_m = \Pi_e + \Pi_{pl}$. There is a threshold, $\bar{\lambda}_6$, at which $\frac{\partial \Pi_m^*}{\partial \theta} = \frac{\partial \Pi_{e,m}^*}{\partial \theta}$, with Π^* the profit of the exchange when it is a monopoly. For $\lambda > \bar{\lambda}_6$, $\frac{\partial \Pi_m^*}{\partial \theta} > \frac{\partial \Pi_{e,m}^*}{\partial \theta}$ and the signal precision set by the merged exchange is higher than in the monopoly case. For $\lambda < \bar{\lambda}_6$, $\frac{\partial \Pi_m^*}{\partial \theta} < \frac{\partial \Pi_{e,m}^*}{\partial \theta}$ and the signal precision set by the merged exchange is smaller than in the benchmark case.